

□  $P(E|D) = 0.95$ ,  $P(D) = 0.005$

$$P(\bar{D}) = 0.995$$

$$P(E|\bar{D}) = 0.01$$

Note Title

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Q:  $P(D|E)$  ?

$$\begin{aligned} P(D|E) &= \frac{P(D \cap E)}{P(E)} = \frac{P(E|D) \cdot P(D)}{P(E)} \\ &= \frac{P(E|D) \cdot P(D)}{P(E|D) \cdot P(D) + P(E|\bar{D}) \cdot P(\bar{D})} \\ &= \frac{0.95 \times 0.005}{0.95 \times 0.005 + 0.01 \times 0.995} = 0.323 \end{aligned}$$

✓  $P(E|S) = \prod P(w_i|S)$ ,  $P(E|H) = \prod P(w_i|H)$  ← assume independence among keywords

$$P(\text{dollar}|S) = 0.2, \quad P(\text{dollar}|H) = 0.05$$

$$P(\text{cheap}|S) = 0.5, \quad P(\text{cheap}|H) = 0.01$$

$$P(S) = 0.1, \quad P(H) = 0.9$$

$E: \{ \text{cheap, dollar} \}$

Q:  $P(S|E)?$

→  $P(\text{dollar}|S) \times P(\text{cheap}|S)$   $P(H|E)?$

$$P(S|E) = \frac{P(E|S) \cdot P(S)}{P(E|S) \cdot P(S) + P(E|H) \cdot P(H)} = 0.957$$

$$P(H|E) = \frac{P(E|H) \cdot P(H)}{P(E)} = 0.043 \quad \text{high threshold e.g. 90\%}$$

$n = 35$  r.v.  $X = \#$  of active users at current time

$p = 0.1$   $X \sim B(n, p)$

$$P(\text{Congestion}) = P(\text{more than 10 active users})$$

$$= P(X > 10) = 1 - P(X \leq 10)$$

$$= P(X=0) + P(X=1) + \dots + P(X=10)$$

$$= 0.0004$$

$$P(X=k) = \binom{n}{k} p^k (1-p)^{n-k}$$